

Our Lady of the Assumption Catholic Primary School





KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns. By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively. Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single diait.

Children develop column methods to support multiplications in these cases.

For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.



	Year 5				
	Concrete	Pictorial	Abstract		
Year 5 Addition					
Column addition with whole numbers	Use place value equipment to represent additions. Add a row of counters onto the place value grid to show 15,735 + 4,012.	Represent additions, using place value equipment on a place value grid alongside written methods. TTh Th Th H T O 2 0 1 5 3 + 1 9 1 7 5 3 9 3 2 8	Use column addition, including exchanges. TTh Th		
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving. FIR.579 £28,370 £16,725	Use approximation to check whether answers are reasonable. TTh Th H T O 2 3 4 0 5 2 3 4 0 5 + 7 8 9 2 2 0 2 9 7 + 7 8 9 2 3 1 2 9 7		



Adding tenths

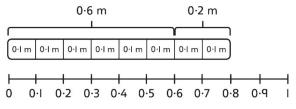
Link measure with addition of decimals.

Two lengths of fencing are 0.6 m and 0.2 m.

How long are they when added together?



Use a bar model with a number line to add tenths.



$$0.6 + 0.2 = 0.8$$

6 tenths + 2 tenths = 8 tenths

Understand the link with adding fractions.

$$\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$$

6 tenths + 2 tenths = 8 tenths 0.6 + 0.2 = 0.8

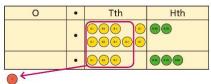
Adding decimals using column addition

Use place value equipment to represent additions.

Show 0·23 + 0·45 using place value counters.

Use place value equipment on a place value grid to represent additions.

Represent exchange where necessary.



O · Tth Hth

0 · 9 2

+ 0 · 3 3

1 · 2 5

Include examples where the numbers of decimal places are different.

0	•	Tth	Hth
00000	•		
0	•	<u></u>	

O · Tth Hth

5 · 0 0

+ I · 2 5

6 · 2 5

Add using a column method, ensuring that children understand the link with place value.

Include exchange where required, alongside an understanding of place value.

Include additions where the numbers of decimal places are different.

$$3.4 + 0.65 = ?$$



V F			
Year 5 Subtraction			
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. 2,250 – 1,070	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required. 15,735 - 2,582 = 13,153 TTh Th H T O TTh Th H T O T S S Subtract the I0s. Exchange I hundred for I0 tens. TTh Th H T O T S S S S S S S S S S S S S S S S S	Use column subtraction methods with exchange where required. TTh Th H T O S Z O Q T - 8 5 3 4 4 3 5 6 3 62,097 - 18,534 = 43,563
Checking strategies and representing subtractions		Bar models represent subtractions in problem contexts, including 'find the difference'. Athletics Stadium 75,450 Hockey Centre 42,300 Velodrome 15,735	Children can explain the mistake made when the columns have not been ordered correctly. Bello's working Th Th H T 0 1 7 8 7 7 1 4 0 1 2 2 1 8 8 9 Use approximation to check calculations. I calculated 18,000 + 4,000 mentally to check my subtraction.



Choosing efficient methods			To subtract two large numbers that are close, children find the difference by counting on. $2,002 - 1,995 = ?$ Use addition to check subtractions. I calculated $7,546 - 2,355 = 5,191$. I will check using the inverse.
Subtracting decimals	Explore complements to a whole number by working in the context of length. O-49 m I m - m = m 1 - 0-49 = ?	Use a place value grid to represent the stages of column subtraction, including exchanges where required. $5.74 - 2.25 = ?$ $\begin{array}{ c c c c c c c c c c c c c c c c c c c$	Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places. 3.921 - 3.75 = ? O Tth Hth Thth 3 Q Q I - 3 7 5 0 - 3 7 5 0



Year 5 Multiplication			
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'.	Use images to explore examples and non- examples of square numbers.	Understand the pattern of square numbers in the multiplication tables.
	25 is a square number because it is made from 5 rows of 5. Use cubes to explore cube numbers.	8 × 8 = 64 8 ² = 64	Use a multiplication grid to circle each square number. Can children spot a pattern?
	8 is a cube number.	12 is not a square number, because you cannot multiply a whole number by itself to make 12.	
Multiplying by 10, 100 and 1,000	Use place value equipment to multiply by 10, 100 and 1,000 by unitising. 4 × I = 4 ones = 4 4 × I0 = 4 tens = 40 4 × I00 = 4 hundreds = 400	Understand the effect of repeated multiplication by 10.	Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000. H T O T 17 × 10 = 170 17 × 100 = 17 × 10 × 10 = 1,700 17 × 1,000 = 17 × 10 × 10 × 10 = 17,000



Multiplying by
multiples of 10
100 and 1,000

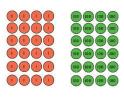
Use place value equipment to explore multiplying by unitising.

5 groups of 3 ones is 15 ones. 5 groups of 3 tens is 15 tens.

So, I know that 5 groups of 3 thousands would be 15 thousands.

Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.





$$6 \times 4 = 24$$

 $6 \times 400 = 2.400$

Use known facts and unitising to multiply.

$$5 \times 4 = 20$$

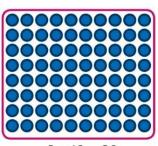
 $5 \times 40 = 200$
 $5 \times 400 = 2,000$
 $5 \times 4,000 - 20,000$

$$5,000 \times 4 = 20,000$$

Multiplying up to 4-digit numbers by a single digit

Explore how to use partitioning to multiply efficiently.

 $8 \times 17 = ?$



$$8 \times 10 = 80$$

$$80 + 56 = 136$$

Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.

Н	T	0
60	000000	000
	00000	000
600	000000	000
©	000000	000
6	00000	000

Use an area model and then add the parts.

Use a column multiplication, including any required exchanges.

 $8 \times 7 = 56$



Multiplying 2-
digit numbers
by 2-digit
numbers

Partition one number into 10s and 1s, then add the parts.

23 × 15 = ?



1 5 0

1 5 0

3 4 5

+ 4 5



 $3 \times 15 = 45$

There are 345 bottles of milk in total.

 $23 \times 15 = 345$

Use an area model and add the parts.

28 × 15 = ?

	20 m	8 m	Н	Т	0
			2	0	0
10 m	$20 \times 10 = 200 \text{ m}^2$	8 × 10 = 80 m ²	1	0	0
				8	0
	- KS		+	4	0
5 m	$20 \times 5 = 100 \text{ m}^2$	$8 \times 5 = 40 \text{ m}^2$	4	2	0
9			_	1	

$$28 \times 15 = 420$$

Use column multiplication, ensuring understanding of place value at each stage.

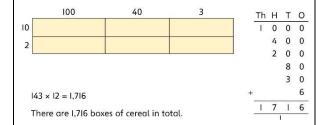
3 4

3 4

- 3	_	-	_			
	9	1	8	34	×	27
	6	8	0	34	×	20
	2	3	8	34	×	7
×		2	7			
		3	4			

Multiplying up to 4-digits by 2-digits

Use the area model then add the parts.



$$143 \times 12 = 1,716$$

Use column multiplication, ensuring understanding of place value at each stage.

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.



			1,274 × 32 = ? First multiply 1,274 by 2. \[\begin{array}{cccccccccccccccccccccccccccccccccccc
Multiplying decimals by 10, 100 and 1,000	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid. Output The Hth Control of the Hth Cont	$1,274 \times 32 = 40,768$ Understand how this exchange is represented on a place value chart. The Heavy Tensor Tenso



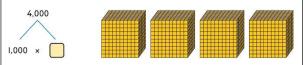
Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number. 24 ÷ 3 = 8 24 ÷ 8 = 3 8 and 3 are factors of 24 because they divide 24 exactly. 24 ÷ 5 = 4 remainder 4. 5 is not a factor of 24 because there is a remainder.	Understand that prime numbers are numbers with exactly two factors. 13 ÷ 1 = 13 13 ÷ 2 = 6 r 1 13 ÷ 4 = 4 r 1 1 and 13 are the only factors of 13. 13 is a prime number.	Understand how to recognise prime and composite numbers. I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder. I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33. I know that 1 is not a prime number, as it has only 1 factor.
Understanding inverse operations and the link with multiplication, grouping and sharing	Use equipment to group and share and to explore the calculations that are present. I have 28 counters. I made 7 groups of 4. There are 28 in total. I have 28 in total. I shared them equally into 7 groups. There are 4 in each group. I have 28 in total. I made groups of 4. There are 7 equal groups.	Represent multiplicative relationships and explore the families of division facts.	Represent the different multiplicative relationships to solve problems requiring inverse operations. 2 ÷ 3 =



Dividing whole
numbers by
10, 100 and
1,000

Use place value equipment to support unitising for division.

4,000 ÷ 1,000

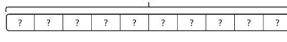


4,000 is 4 thousands.

$$4 \times 1,000 = 4,000$$

So, $4,000 \div 1,000 = 4$

Use a bar model to support dividing by unitising.





380

380 is 38 tens.

 $38 \times 10 = 380$ $10 \times 38 = 380$

So, $380 \div 10 = 38$

Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.

Th	Н	T	0
3	2	0	0

 $3,200 \div 100 = ?$

3,200 is 3 thousands and 2 hundreds.

 $200 \div 100 = 2$

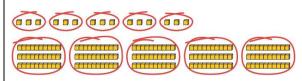
 $3,000 \div 100 = 30$

 $3,200 \div 100 = 32$

So, the digits will move two places to the right.

Dividing by multiples of 10, 100 and 1,000

Use place value equipment to represent known facts and unitising.



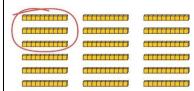
15 ones put into groups of 3 ones. There are 5 groups.

$$15 \div 3 = 5$$

15 tens put into groups of 3 tens. There are 5 groups.

$$150 \div 30 = 5$$

Represent related facts with place value equipment when dividing by unitising.



180 is 18 tens.

18 tens divided into groups of 3 tens. There are 6 groups.

$$180 \div 30 = 6$$

Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.

$$3,000 \div 5 = 600$$

$$3.000 \div 50 = 60$$

$$3,000 \div 500 = 6$$

$$5 \times 600 = 3,000$$

$$50 \times 60 = 3,000$$

$$500 \times 6 = 3,000$$



		12 ones divided into groups of 4. There are 3 groups. 12 hundreds divided into groups of 4 hundreds. There are 3 groups. 1200 ÷ 400 = 3	
Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment. 268 ÷ 2 = ? There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones. 264 ÷ 2 = 134	Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting. The model would need adapting.	Use short division for up to 4-digit numbers divided by a single digit. $ \begin{array}{cccccccccccccccccccccccccccccccccc$



		Work with divisions that require exchange.	
		T O First, lay out the problem. T O How many groups of 4 go	
		How many groups of 4 go into 9 tens? 2 T O Eschange the I ten left 2 T O Exchange the I ten left	
		over for 10 ones. We now have I2 ones.	
		How many groups of 4 go into I2 ones? 3 groups of 4 ones.	
Understanding remainders	Understand remainders using concrete versions of a problem.	Use short division and understand remainders as the last remaining 1s.	In problem solving contexts, represent divisions including remainders with a bar
	80 cakes divided into trays of 6.	T O Lay out the problem as short division. T O How many groups of 6 go	683 136 136 136 136 3
	80 cakes in total. They make 13 groups of 6, with 2 remaining.	6 8 20 into 8 tens? There is Leroup of 6 tens.	683 = 136 × 5 + 3 683 ÷ 5 = 136 r 3
		How many groups of 6 go into 20 ones? There are 3 groups of 6 ones. There are 2 ones remaining.	<u> </u>



Dividing						
decimals b	y					
10, 100 and	d					
1,000						

Understand division by 10 using exchange.

2 ones are 20 tenths.

20 tenths divided by 10 is 2 tenths.

Represent division using exchange on a place value grid.

12-			
0	٠	Tth	Hth
0	٠	<u>00000</u>	
0	•	Tth	Hth
Ø	•	99999 99999 99999	
0	•	Tth	Hth
	•	©©©© ©©©©	

1.5 is 1 one and 5 tenths.

This is equivalent to 10 tenths and 50 hundredths.

10 tenths divided by 10 is 1 tenth. 50 hundredths divided by 10 is 5 hundredths.

1.5 divided by 10 is 1 tenth and 5 hundredths.

 $1.5 \div 10 = 0.15$

Understand the movement of digits on a place value grid.

0	•	Tth	Hth	Thth
0	•	8	5	
0	/•	7 0	8 1	7 5

$$0.85 \div 10 = 0.085$$

0	•	Tth	Hth	Thth
8_	•/	5 _	/	
0	•	0	→8	→5

$$8.5 \div 100 = 0.085$$

Understanding the relationship between fractions and division

Use sharing to explore the link between fractions and division.

1 whole shared between 3 people. Each person receives one-third.



Use a bar model and other fraction representations to show the link between fractions and division.



$$1 \div 3 = \frac{1}{3}$$

Use the link between division and fractions to calculate divisions.

$$5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$$

$$11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$$

