

Our Lady of the Assumption Catholic Primary School



Power Maths calculation policy, Year 3



#### **KEY STAGE 2**

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns. By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2.

Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively. Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single diait.

Children develop column methods to support multiplications in these cases.

For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.

in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.

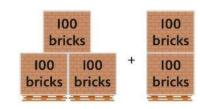


		Year 3	
	Concrete	Pictorial	Abstract
Year 3 Addition			
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens.  Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use a place value grid to support the structure of numbers to 1,000.  Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.	Represent the parts of numbers to 1,000 using a part-whole model.  215 = 200 + 10 + 5  Recognise numbers to 1,000 represented on a number line, including those between intervals.



## Adding 100s

Use known facts and unitising to add multiples of 100.



Use known facts and unitising to add multiples of 100.





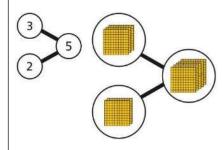
Use number bonds to add the Is.

5 + 4 = 9

Use known facts and unitising to add multiples of 100.

Represent the addition on a number line.

Use a part-whole model to support unitising.



$$3 + 2 = 5$$
  
 $300 + 200 = 500$ 

## 3-digit number + 1s, no exchange or bridging

Use number bonds to add the 1s.



214 + 4 = ?

Now there are 4 + 4 ones in total. 4 + 4 = 8

214 + 4 = 218

Use number bonds to add the 1s.

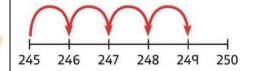
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2	4	q

$$245 + 4$$
  
 $5 + 4 = 9$ 

$$245 + 4 = 249$$

Understand the link with counting on.

$$245 + 4$$



Use number bonds to add the 1s and understand that this is more efficient and less prone to error.

$$245 + 4 = ?$$

I will add the 1s.

$$5 + 4 = 9$$

So, 
$$245 + 4 = 249$$

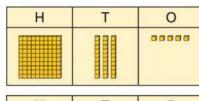


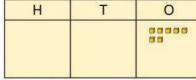
3-digit number + 1s with exchange

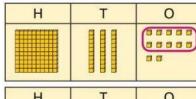
Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.

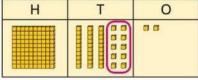
Children should explore this using unitised objects or physical apparatus.

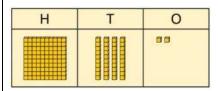
Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.





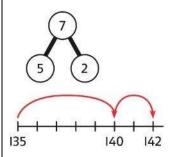






$$135 + 7 = 142$$

Understand how to bridge by partitioning to the 1s to make the next 10.



Ensure that children understand how to add 1s bridging a 100.

$$198 + 2 + 3 = 203$$



# 3-digit number + 10s, no exchange

Calculate mentally by forming the number bond for the 10s.





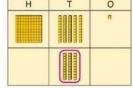
234 + 50There are 3 tens and 5 tens altogether. 3 + 5 = 8

In total there are 8 tens.

234 + 50 = 284

Calculate mentally by forming the number bond for the 10s.





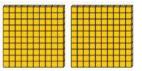
Calculate mentally by forming the number bond for the 10s.

I know that 5 + 4 = 9

So, 
$$50 + 40 = 90$$
  
 $753 + 40 = 793$ 

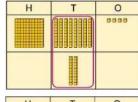
## 3-digit number + 10s, with exchange

Understand the exchange of 10 tens for 1 hundred.





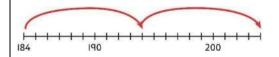
Add by exchanging 10 tens for 1 hundred.





$$184 + 20 = 204$$

Understand how the addition relates to counting on in 10s across 100.



Use number bonds within 20 to support efficient mental calculations.



3-digit number + 2-digit number	Use place value equipment to make and combine groups to model addition.	Use a place value grid to organise thinking and adding of 1s, then 10s.	Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation.
3-digit number + 2-digit number, exchange required	Use place value equipment to model addition and understand where exchange is required.  Use place value counters to represent	Represent the required exchange on a place value grid using equipment.  275 + 16 = ?	Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.
required	Use place value counters to represent 154 + 72.  Use this to decide if any exchange is required.  There are 5 tens and 7 tens. That is 12 tens so I will exchange.	H T O  275 + 16 = 291  Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value.	$ \begin{array}{c ccccc}  & H & T & O \\ \hline 2 & 7 & 5 \\ + & & 1 & 6 \\ \hline  & & & 1 \end{array} $ $ \begin{array}{c ccccccc}  & H & T & O \\ \hline  & 2 & 7 & 5 \\ + & & & 1 & 6 \\ \hline  & & & & & & & \\ \hline  & & & & & \\ \hline  & & & $
		Children should be encouraged at every stage to select methods that are accurate and efficient.	



3-digit number + 3-digit

number, no

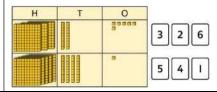
exchange

Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.

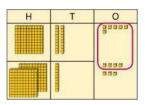
Represent the place value grid with equipment to model the stages of column addition.

Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.

326 + 541 is represented as:

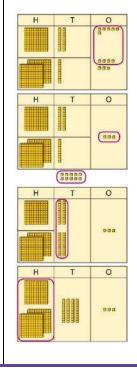


3-digit number + 3-digit number, exchange required Use place value equipment to enact the exchange required.



There are 13 ones.
I will exchange 10 ones for 1 ten.

Model the stages of column addition using place value equipment on a place value grid.



Use column addition, ensuring understanding of place value at every stage of the calculation.



$$126 + 217 = 343$$

Note: Children should also study examples where exchange is required in more than one column, for example 185 + 318 = ?

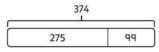


Representing
addition
problems, and
selecting
appropriate
methods

Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps.

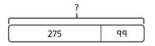
These representations will help them to select appropriate methods.

Children understand and create bar models to represent addition problems.



275 + 99 = 374

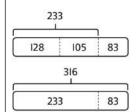
Use representations to support choices of appropriate methods.



I will add 100, then subtract 1 to find the solution.

128 + 105 + 83 = ? I need to add three numbers.

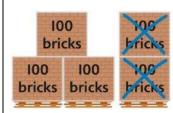
$$128 + 105 = 233$$



## Year 3 Subtraction

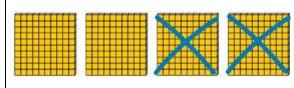
## Subtracting 100s

Use known facts and unitising to subtract multiples of 100.



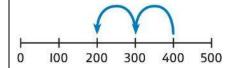
$$5 - 2 = 3$$
  
 $500 - 200 = 300$ 

Use known facts and unitising to subtract multiples of 100.



$$4 - 2 = 2$$
  
 $400 - 200 = 200$ 

Understand the link with counting back in 100s.



$$400 - 200 = 200$$

Use known facts and unitising as efficient and accurate methods.

I know that 7 - 4 = 3. Therefore, I know that 700 - 400 = 300.



3-digit number
– 1s, no
exchange

Use number bonds to subtract the 1s.



$$214 - 3 = ?$$



$$4 - 3 = 1$$
  
 $214 - 3 = 211$ 

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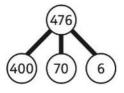
Use number bonds to subtract the 1s.

$$319 - 4 = ?$$

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3	- 1	q

Understand the link with counting back using a number line.

Use known number bonds to calculate mentally.



$$6 - 4 = 2$$
  
 $476 - 4 = 472$ 

## 3-digit number - 1s, exchange or bridging required

Understand why an exchange is necessary by exploring why 1 ten must be exchanged.

Use place value equipment.

Represent the required exchange on a place value grid.

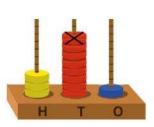
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Calculate mentally by using known bonds.



## 3-digit number – 10s, no exchange

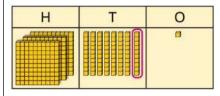
Subtract the 10s using known bonds.



8 tens with 1 removed is 7 tens.

$$381 - 10 = 371$$

Subtract the 10s using known bonds.



Use known bonds to subtract the 10s mentally.

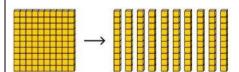
$$372 - 50 = ?$$

$$70 - 50 = 20$$

So, 
$$372 - 50 = 322$$

# 3-digit number – 10s, exchange or bridging required

Use equipment to understand the exchange of 1 hundred for 10 tens.

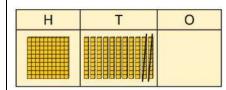


Represent the exchange on a place value grid using equipment.

$$210 - 20 = ?$$

Н	T	0

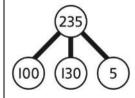
I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.



$$210 - 20 = 190$$

Understand the link with counting back on a number line.

Use flexible partitioning to support the calculation.

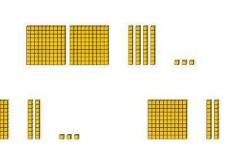


$$235 = 100 + 130 + 5$$
  
 $235 - 60 = 100 + 70 + 5$   
 $= 175$ 

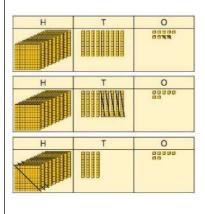


3-digit number
- up to 3-digit
number

Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.



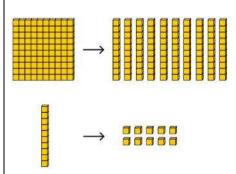
Represent the calculation on a place value grid.



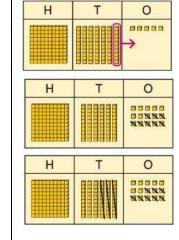
Use column subtraction to calculate accurately and efficiently.

3-digit number
- up to 3-digit
number,
exchange
required

Use equipment to enact the exchange of 1 hundred for 10 tens, and 1 ten for 10 ones.



Model the required exchange on a place value grid.



Use column subtraction to work accurately and efficiently.

If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly.

Children should also understand how to exchange in calculations where there is a zero in the 10s column.





Representing subtraction problems		Use bar models to represent subtractions.  'Find the difference' is represented as two bars for comparison.  Team A 454 Team B 128 ?  Bar models can also be used to show that a part must be taken away from the whole.	Children use alternative representations to check calculations and choose efficient methods.  Children use inverse operations to check additions and subtractions. The part-whole model supports understanding.  I have completed this subtraction.  525 - 270 = 255 I will check using addition.
Year 3 Multiplication			
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non-examples using objects.	Children recognise that arrays demonstrate commutativity.  This is 3 groups of 4. This is 4 groups of 3.	Children understand the link between repeated addition and multiplication. $ \begin{array}{cccccccccccccccccccccccccccccccccc$



Children recognise that arrays can be used
to model commutative multiplications.



I can see 3 groups of 8. I can see 8 groups of 3.

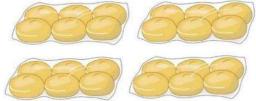
A bar model may represent multiplications as equal groups.

 $6 \times 4 = 24$ 

# Using commutativity to support understanding of the timestables

Understand how to use times-tables facts flexibly.

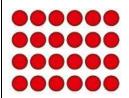




There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls.

I can use  $6 \times 4 = 24$  to work out both totals.

Understand how times-table facts relate to commutativity.



 $6 \times 4 = 24$  $4 \times 6 = 24$  Understand how times-table facts relate to commutativity.

I need to work out 4 groups of 7.

I know that  $7 \times 4 = 28$ 

so, I know that

4 groups of 7 = 28and 7 groups of 4 = 28.



**Understanding** and using ×3, ×2. ×4 and ×8 tables.

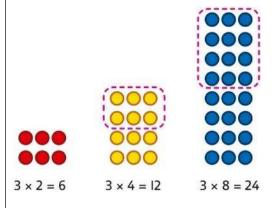
Children learn the times-tables as 'groups of', but apply their knowledge of commutativity.



I can use the ×3 table to work out how many keys.

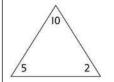
I can also use the ×3 table to work out how many batteries.

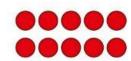
Children understand how the ×2, ×4 and ×8 tables are related through repeated doubling.



Understand how unitising 10s supports

Children understand the relationship between related multiplication and division facts in known times-tables.





 $2 \times 5 = 10$  $5 \times 2 = 10$  $10 \div 5 = 2$  $10 \div 2 = 5$ 

**Using known** facts to multiply 10s, for example  $3 \times 40$ 

Explore the relationship between known times-tables and multiples of 10 using place value equipment.

Make 4 groups of 3 ones.

Make 4 groups of 3 tens.

What is the same?

What is different?

















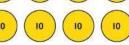


multiplying by multiples of 10.



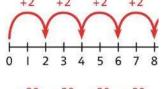


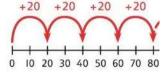




4 groups of 2 ones is 8 ones. 4 groups of 2 tens is 8 tens.

Understand how to use known times-tables to multiply multiples of 10.





$$4 \times 2 = 8$$
$$4 \times 20 = 80$$



Multiplying a 2-digit number by a 1-digit number Understand how to link partitioning a 2-digit number with multiplying.

Each person has 23 flowers.

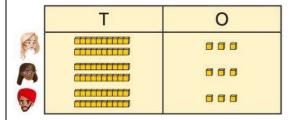
Each person has 2 tens and 3 ones.



There are 3 groups of 2 tens.

There are 3 groups of 3 ones.

Use place value equipment to model the multiplication context.

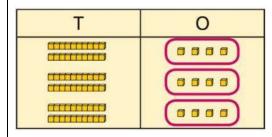


There are 3 groups of 3 ones.

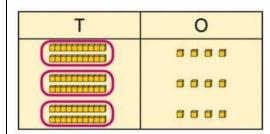
There are 3 groups of 2 tens.

Use place value to support how partitioning is linked with multiplying by a 2-digit number.

$$3 \times 24 = ?$$



$$3 \times 4 = 12$$



$$3 \times 20 = 60$$

$$60 + 12 = 72$$

$$3\times 24=72$$

Use addition to complete multiplications of 2-digit numbers by a 1-digit number.

$$4 \times 13 = ?$$

$$4 \times 3 = 12$$

$$4 \times 10 = 40$$

$$12 + 40 = 52$$

$$4 \times 13 = 52$$

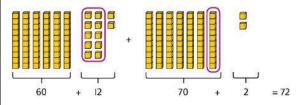


Multiplying a 2-digit number by a 1-digit number, expanded column method Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.

$$3 \times 24 = ?$$

$$3 \times 20 = 60$$

$$3 \times 4 = 12$$



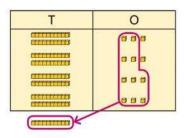
$$3 \times 24 = 60 + 12$$

$$3 \times 24 = 70 + 2$$

$$3 \times 24 = 72$$

Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.

$$4 \times 23 = ?$$



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$$4 \times 23 = 92$$

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(II)	000
(e) (e)	000
(10) (10)	000
00	000

$$5 \times 23 = ?$$

$$5 \times 3 = 15$$

$$5 \times 20 = 100$$

$$5 \times 23 = 115$$

Children may write calculations in expanded column form, but must understand the link with place value and exchange.

Children are encouraged to write the expanded parts of the calculation separately.

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$$5 \times 28 = ?$$



Year 3 Division			
Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions.  24 divided into groups of 8. There are 3 groups of 8.	Use knowledge of known times-tables to calculate divisions.	Use knowledge of known times-tables to calculate divisions.  I need to work out 30 shared between 5.  I know that $6 \times 5 = 30$ so I know that $30 \div 5 = 6$ .  A bar model may represent the relationship between sharing and grouping. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$



	I	1	
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects	Use images to explain remainders.	Understand that the remainder is what cannot be shared equally from a set.
remainuers	cannot be divided equally any further.	00000 0	Calliot be shared equally from a set.
	, , ,	••••	22 ÷ 5 = ?
		••••	3 × 5 = 15
		00 . 5 . 4	$\begin{array}{c} 3 \times 5 = 15 \\ 4 \times 5 = 20 \end{array}$
	There are 13 sticks in total. There are 3 groups of 4, with 1 remainder.	22 ÷ 5 = 4 remainder 2	$5 \times 5 = 25 \dots$ this is larger than 22
	There are 3 groups of 4, with 1 remainder.		So, 22 ÷ 5 = 4 remainder 2
Using known facts to divide	Use place value equipment to understand how to divide by unitising.	Divide multiples of 10 by unitising.	Divide multiples of 10 by a single digit using known times-tables.
multiples of 10	Make 6 ones divided by 3.		180 ÷ 3 = ?
			180 is 18 tens.
	Now make 6 tens divided by 3.	12 tens shared into 3 equal groups.	18 divided by 3 is 6.
		4 tens in each group.	18 tens divided by 3 is 6 tens.
			18 ÷ 3 = 6 180 ÷ 3 = 60
	What is the same? What is different?		
2-digit number divided by 1-digit number,	Children explore dividing 2-digit numbers by using place value equipment.	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate.
no remainders			
		42)	68
		40 2	60 8
		40 2	
		CHICAGO	60 ÷ 2 = 30
	48 ÷ 2 = ?		8 ÷ 2 = 4
			30 + 4 = 34 68 ÷ 2 = 34
			00 · 2 - 37







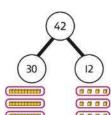


Then divide the 1s.





I need to partition 42 differently to divide by 3.



$$42 = 30 + 12$$

Children partition flexibly to divide where appropriate.

$$42 \div 3 = ?$$

$$42 = 40 + 2$$

I need to partition 42 differently to divide by 3.

$$42 = 30 + 12$$

$$30 \div 3 = 10$$

$$12 \div 3 = 4$$

$$10 + 4 = 14$$

$$42 \div 3 = 14$$

## 2-digit number divided by 1-digit number, with remainders

Use place value equipment to understand the concept of remainder.

Make 29 from place value equipment. Share it into 2 equal groups.





There are two groups of 14 and 1 remainder.

Use place value equipment to understand the concept of remainder in division.

$$29 \div 2 = ?$$





Partition to divide, understanding the remainder in context.

67 children try to make 5 equal lines.

$$67 = 50 + 17$$

$$50 \div 5 = 10$$

$$17 \div 5 = 3$$
 remainder 2

$$67 \div 5 = 13 \ remainder \ 2$$

There are 13 children in each line and 2 children left out.